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ADDITIONAL CORRIGENDA TO VOL. 104, PART C, 1957

Page 500. In the caption to Fig. 6 R_d /time should read: R_d/I_A .

Page 517. The third term on the right-hand side of eqn. (43) should read: $(L_i + \bar{L}_k)G^2_{xa}$

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